

# MEMORIAL DE CÁLCULO DE FÍSICA ESTÁTICA E CIRCUITOS ELÉTRICOS DO PROJETO INTEGRADO DA PONTE DE MARCARRÃO

## Curso de Engenharia Civil – EAD

Charles Dias de Moraes Filho - RA 25000761

Luciana Matos Araújo Fossa – RA 24000565

Nickolas Pinto de Oliveira - RA 24000515

Nailla Julia do Lago - RA 24001255

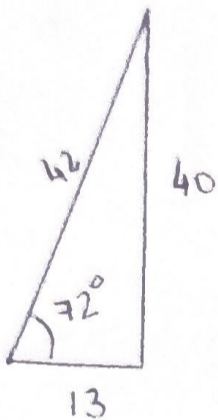
① TIPO DE ESTRUTURA

$$2 \cdot n = B + R$$

$$2 \cdot 16 = 29 + 3$$

$$\boxed{32 = 32}$$

② CÁLCULO DO ÂNGULO



$$\text{tg} \frac{40}{13} = 3.076$$

$$\text{tg}^{-1} 3.076 = 72^\circ$$

$$\cos 72^\circ = 0.309$$

$$\text{sen} 72^\circ = 0.951$$

③ CÁLCULO DAS REAÇÕES DE APOIO

$$\sum F_x = 0$$

$$H_A = 0$$

$$\sum F_y = V_A - 200 + V_Q = 0$$

$$\sum F_y = V_A + V_Q = 200$$

$$V_A + 100 = 200$$

$$V_A = 200 - 100$$

$$\boxed{V_A = 100}$$

FORÇA DE MOMENTO

$$\sum M_A = -200 \times 52 + V_R \times 104 = 0$$

$$-10400 + 104 \cdot V_R = 0$$

$$104 \cdot V_R = 10400$$

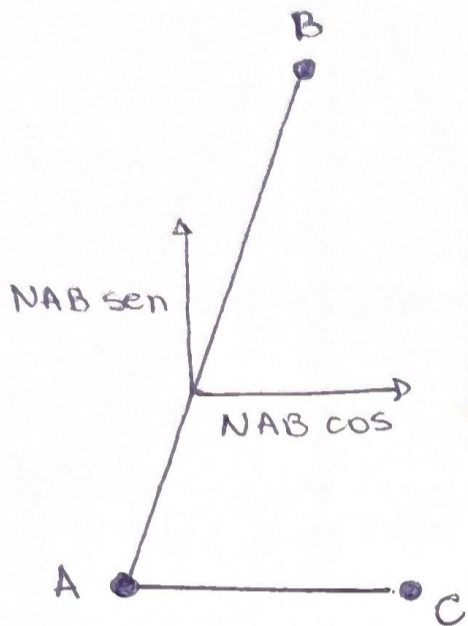
$$V_R = \frac{10400}{104}$$

$$104$$

$$\boxed{V_R = 100 \text{ N}}$$

## ④ CÁLCULO DOS NÓS

NÓ (A)



FORÇAS VERTICAIS

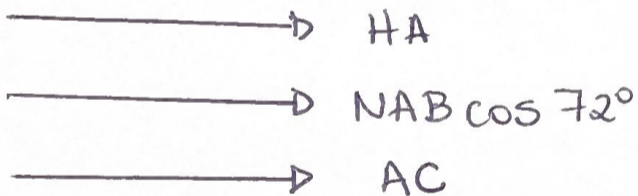


$$\begin{aligned} V_A + N_{AB} \cdot \sin 72^\circ &= 0 \\ 100 + N_{AB} \cdot 0,95 &= 0 \\ 0,95 N_{AB} &= -100 \\ N_{AB} &= \frac{-100}{0,95} \end{aligned}$$

$$N_{AB} = -105,26$$

COMPRESSÃO

FORÇAS HORIZONTAIS

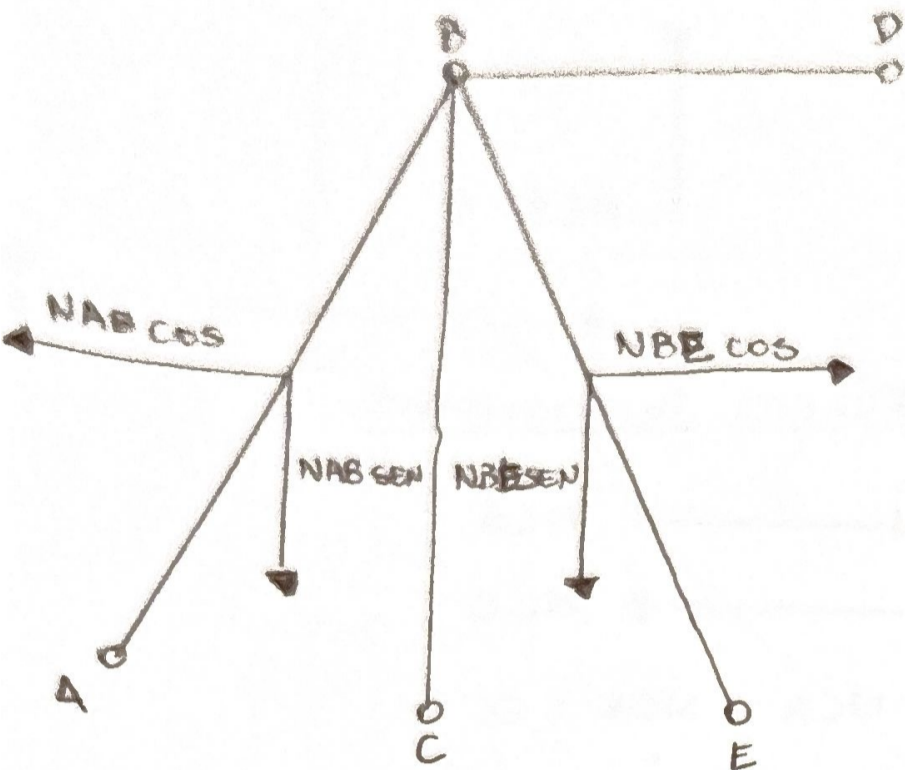


$$\begin{aligned} H_A + N_{AB} \cos 72^\circ + N_{AC} &= 0 \\ 0 + (-105,26 \times 0,31) + N_{AC} &= 0 \\ -32,63 + N_{AC} &= 0 \end{aligned}$$

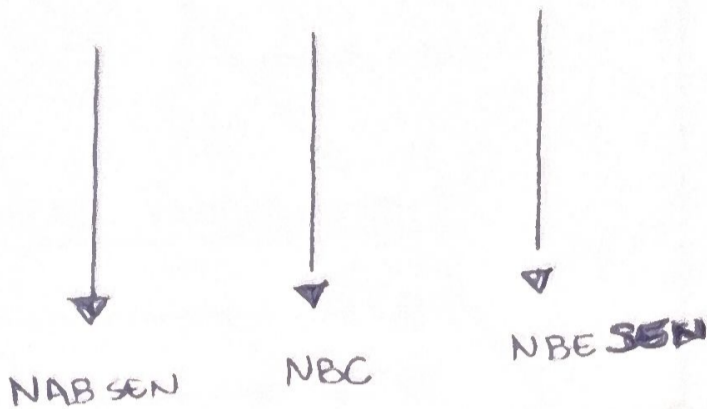
$$N_{AC} = 32,63$$

TRAÇÃO

NO' (B)



FORÇAS VERTICAIS



$$\begin{aligned}
 & - NAB \times \text{sen } 72^\circ - NBC - NBE \text{ sen } 72^\circ = 0 \\
 & - (-105,26 \times 0,95) - NBC - NBE \times 0,95 = 0 \\
 & 99,99 - 0 - NBE \times 0,95 = 0 \\
 & - NBE \times 0,95 = -99,99 \\
 & - NBE = \frac{-99,99}{0,95}
 \end{aligned}$$

$$- NBE = -105,26 \quad (\times -1)$$

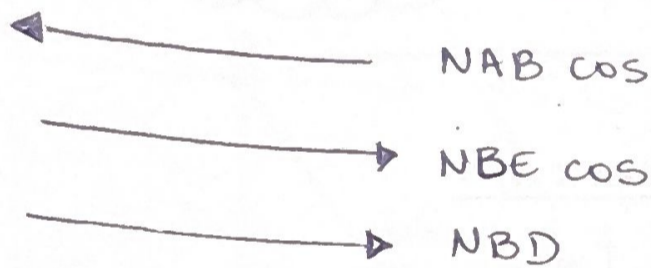
$$\boxed{NBE = 105,26}$$

TRAÇÃO

$$\begin{aligned}
 & - NAB \text{ sen } 72^\circ - NBC - NBE \text{ sen } 72^\circ = 0 \\
 & - (-105,26 \times 0,95) - NBC - (105,26 \times 0,95) = 0 \\
 & + 99,99 - NBC - 99,99 = 0 \\
 & - NBC = 0
 \end{aligned}$$

$$\boxed{NBC = 0}$$

FORÇAS HORIZONTAIS

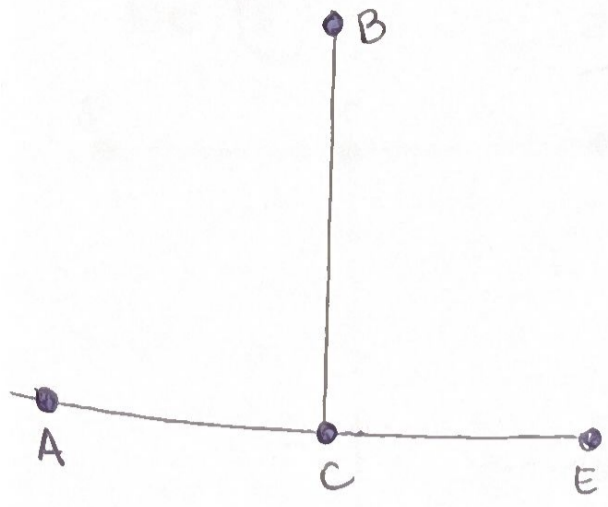


$$\begin{aligned}
 & - NAB \times \text{cos } 72^\circ + NBE \text{ cos } 72^\circ + NBD = 0 \\
 & - (-105,26 \times 0,31) + (105,26 \times 0,31) + NBD = 0 \\
 & + 32,63 + 32,63 + NBD = 0 \\
 & 65,26 + NBD = 0
 \end{aligned}$$

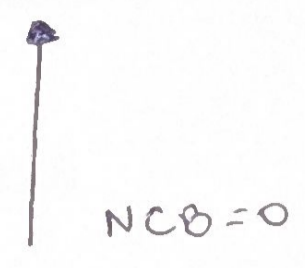
$$\boxed{NBD = -65,26}$$

COMPRESSÃO

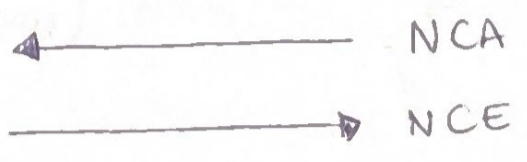
NO (C)



FORÇAS VERTICAIS



FORÇAS HORIZONTAIS



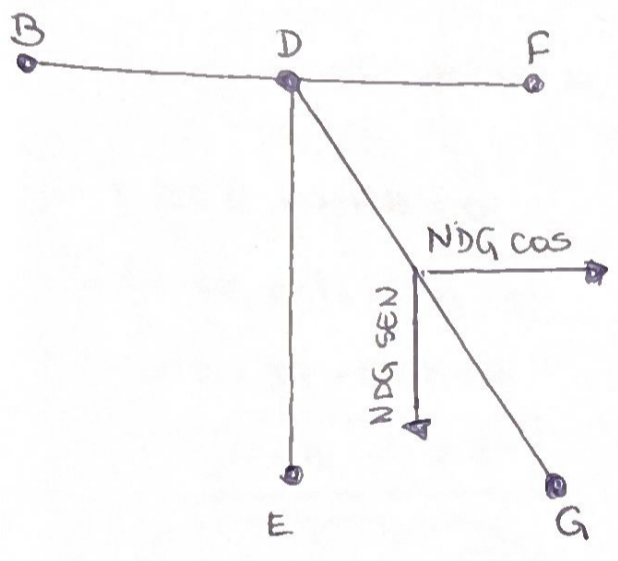
$$-NCA + NCE = 0$$

$$-(32.63) + NCE = 0$$

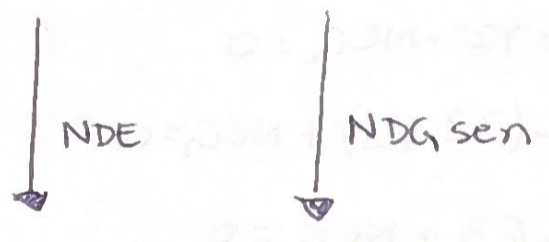
$$\boxed{NCE = 32.63}$$

TRACÃO

NO' (D)



FORÇAS VERTICAIS



$$-NDE - NDG \times \text{sen } 72^\circ = 0$$

$$-NDE - (105.26 \times 0.95) = 0$$

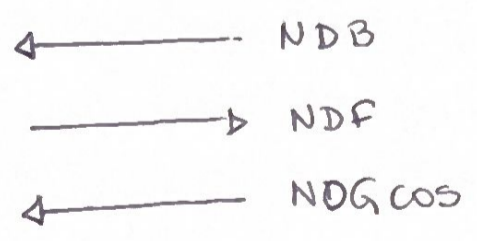
$$-NDE - 99.99 = 0$$

$$-NDE = 99.99 \quad (\times -1)$$

$$\boxed{NDE = -99.99}$$

COMPRESSÃO

FORÇAS HORIZONTAIS



$$-NDB + NDF + NDG \cos 72^\circ = 0 \quad \rightarrow$$

$$-(-65.26) + NDF + (105.26 \times 0.31) = 0$$

$$+65.26 + NDF + 32.63 = 0$$

$$\boxed{NDF = -97.89}$$

COMPRESSÃO

$$-NDB + NDF + NDG \times \cos 72^\circ = 0$$

$$-(-65.26) + (-97.89) + NDG \times 0.31 = 0$$

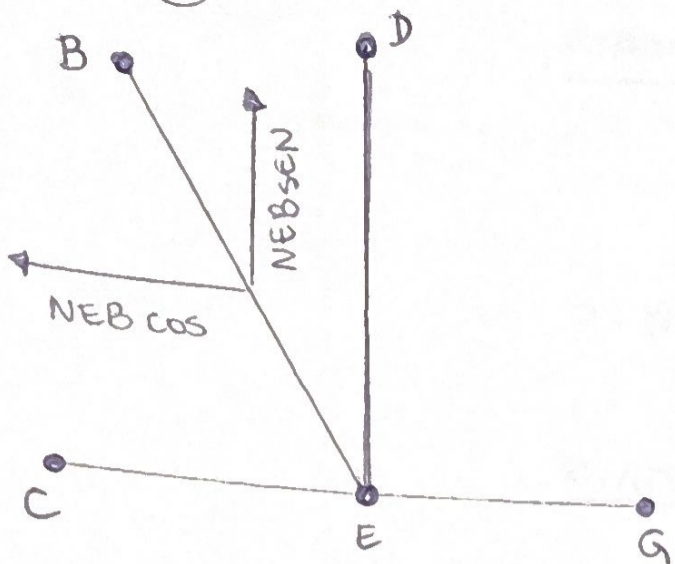
$$+65.26 - 97.89 + NDG \times 0.31 = 0$$

$$-32.63 + NDG \times 0.31$$

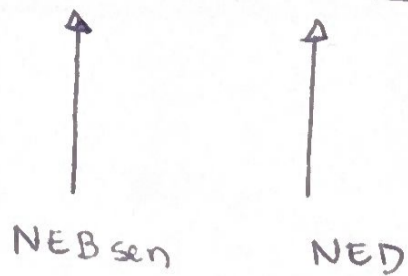
$$NDG = \frac{32.63}{0.31}$$

$$\boxed{NDG = 105.26}$$

TRACÃO



FORÇAS VERTICAIS



$$NEB \times \text{sen} 72^\circ + NED = 0$$

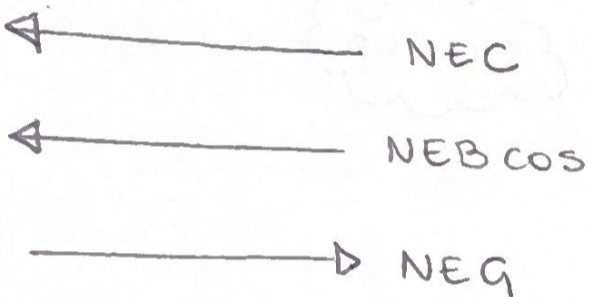
$$(105.26 \times 0.95) + NED = 0$$

$$99.99 + NED = 0$$

$$NED = -99.99$$

COMPRESSÃO

FORÇAS HORIZONTAIS



$$-NEC - NEB \times \text{cos} 72^\circ + NEG = 0$$

$$-(105.26 \times 0.31) - (32.63) + NEG = 0$$

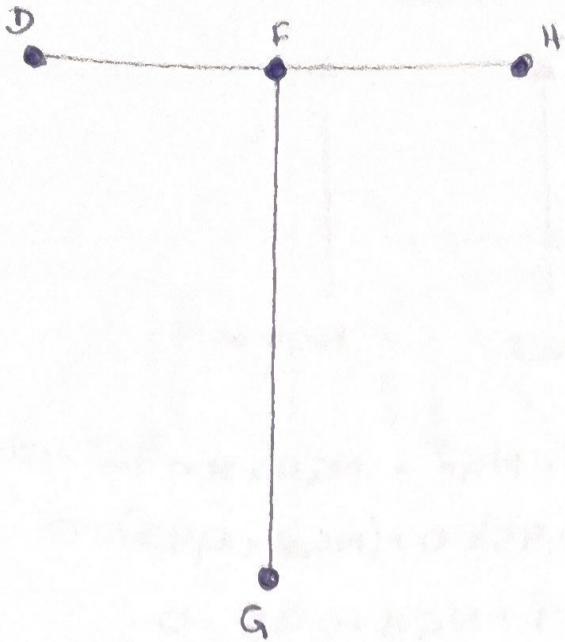
$$-32.63 - 32.63 + NEG = 0$$

$$-65.26 + NEG = 0$$

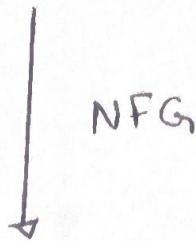
$$NEG = 65.26$$

TRAÇÃO

No' (F)

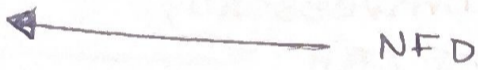


FORÇAS VERTICAIS



$NFG = 0$

FORÇAS HORIZONTAIS



$- NFD + NFH = 0$

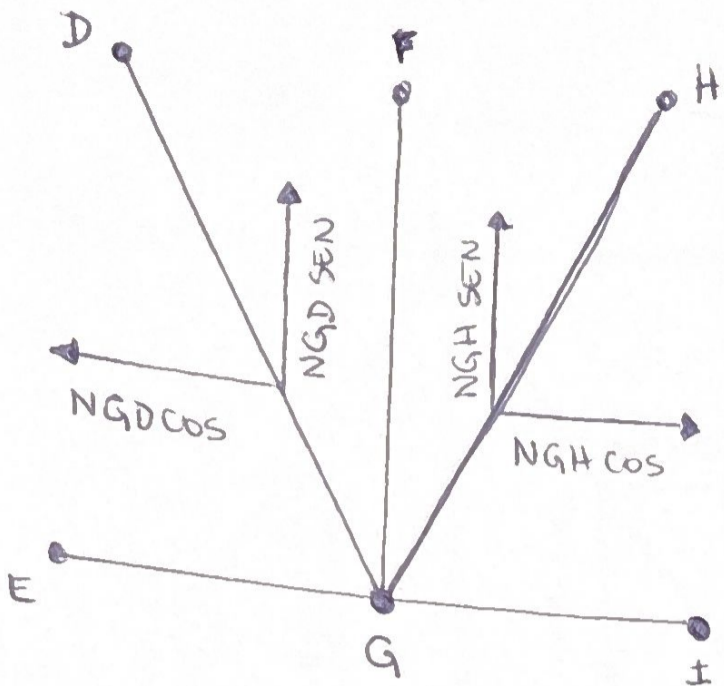
$- (-97,89) + NFH = 0$

$+ 97,89 + NFH = 0$

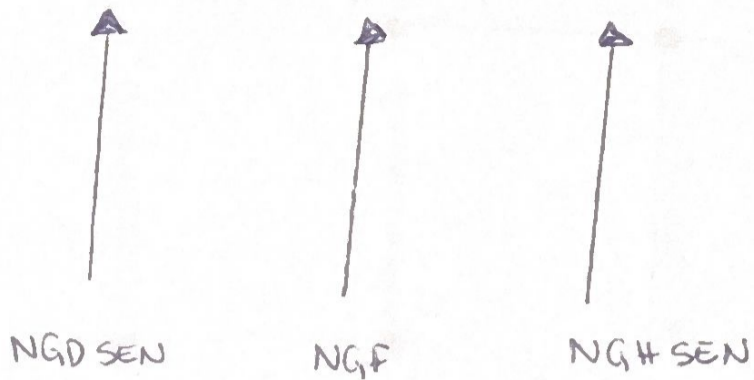
$NFH = -97,89$
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COMPRESSÃO

NO' (G)



FORÇAS VERTICAIS



$$NGD \text{ sen } 72^\circ + NGF + NGH \times \text{sen } 72^\circ = 0$$

$$(105.26 \times 0.95) + 0 + (NGH \times 0.95) = 0$$

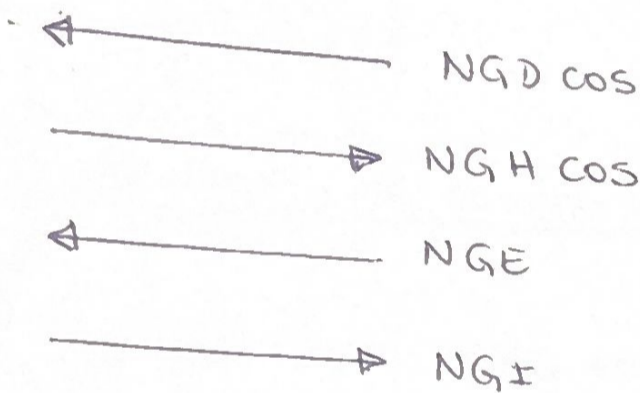
$$99.99 + NGH \times 0.95 = 0$$

$$NGH = \frac{-99.99}{0.95}$$

$$NGH = -105.26$$

COMPRESSÃO

FORÇAS HORIZONTAIS



$$-NGD \times \cos 72^\circ + NGH \times \cos 72^\circ + NGE + NGI = 0$$

$$-NGD \times 0.31 + (-105.26 \times 0.31) - (65.26) + NGI = 0$$

$$-105.26 \times 0.31 - 105.26 \times 0.31 - 65.26 + NGI = 0$$

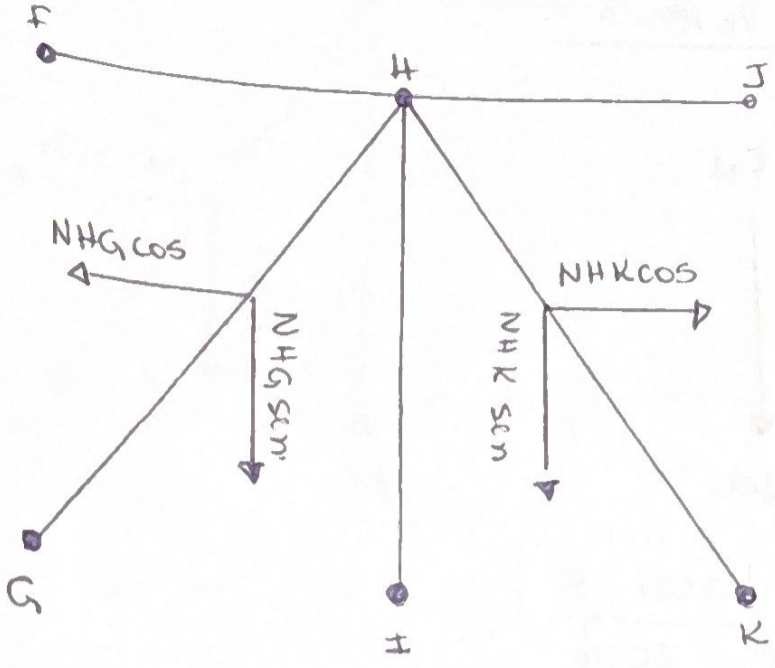
$$-32.63 - 32.63 - 65.26 + NGI = 0$$

$$-130.52 + NGI = 0$$

$$NGI = 130.52$$

TRAÇÃO

Nó (H)



FORÇAS VERTICAIS



$$-NGH \times \text{sen} - NHI - NHK \times \text{sen}$$

$$-(-105.26 \times 0.95) - NHI - (-105.26 \times 0.95) = 0$$

$$+99.99 + 99.99 - NHI = 0$$

$$-NHI = -199.98 \quad (\times -1)$$

$$\boxed{+NHI = 199.98}$$

TRAÇÃO

FORÇAS HORIZONTAIS

- ← NHG cos
- ← NHF
- NHJ
- NHK cos

$$-NHG \times \text{cos} - NHF + NHJ + NHK \text{cos} = 0$$

$$-(-105.26 \times 0.31) - (97.89) + NHJ + (-105.26 \times 0.31) = 0$$

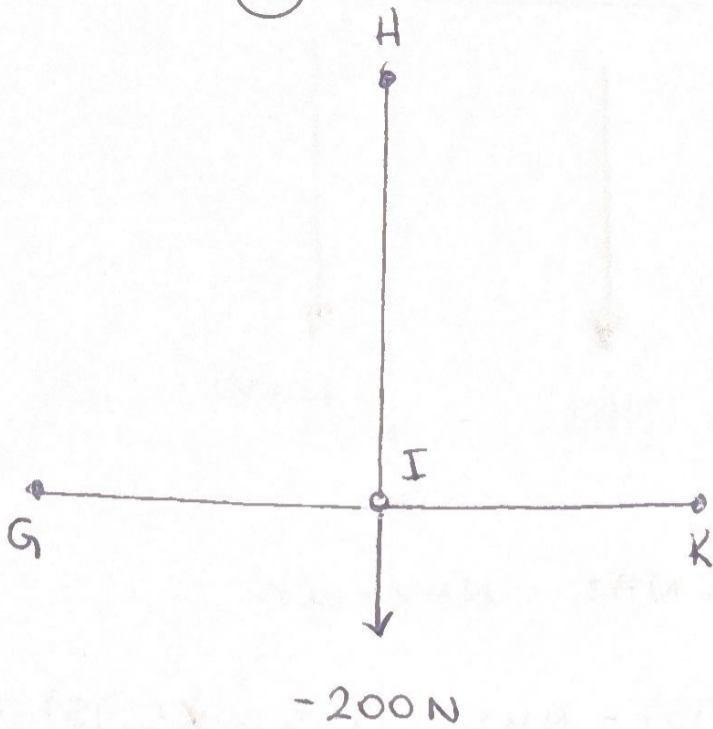
$$+32.63 + 97.89 - 32.63 + NHJ = 0$$

$$97.89 + NHJ = 0$$

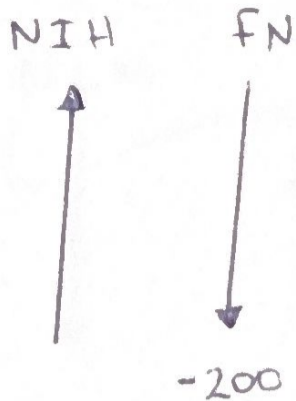
$$\boxed{NHJ = -97.89}$$

COMPRESSÃO

No' (I)



FORÇAS VERTICAIS

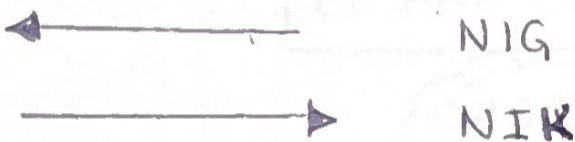


$$NIH - 200 = 0$$

$$\boxed{NIH = 200}$$

TRACÇÃO

FORÇA HORIZONTAL



$$-NIG + NIK = 0$$

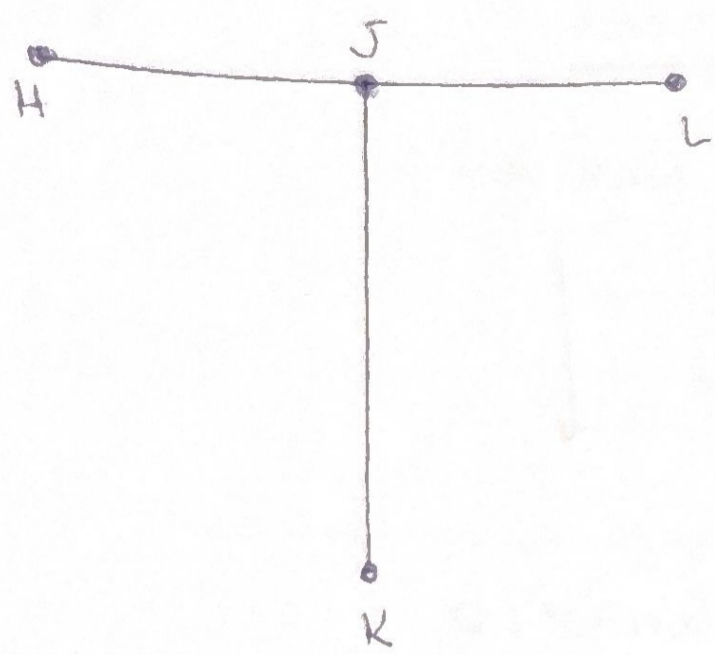
$$-(130.52) + NIK = 0$$

$$-130.52 + NIK = 0$$

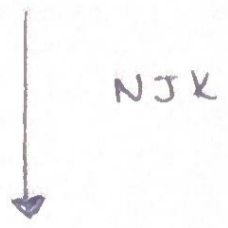
$$\boxed{NIK = 130.52}$$

TRACÇÃO

Nó (J)



FORÇAS VERTICAIS



$$\boxed{NJK = 0}$$

FORÇAS HORIZONTAIS



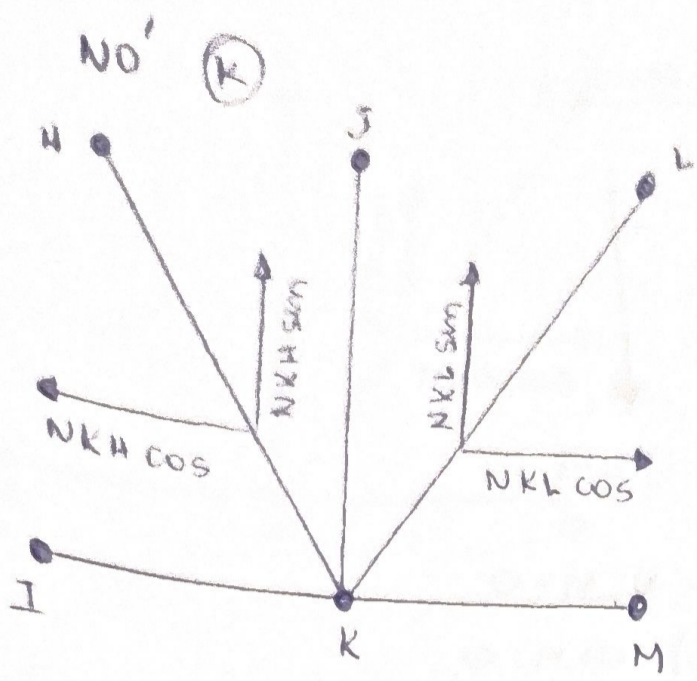
$$-NJH + NJL = 0$$

$$-(-97.89) + NJL = 0$$

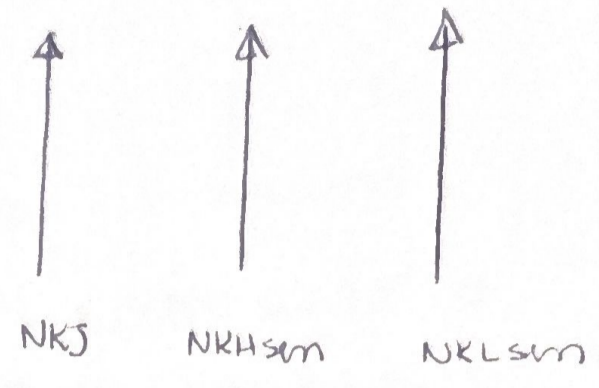
$$+ 97.89 + NJL = 0$$

$$\boxed{NJL = -97.89}$$

COMPRESSÃO



FORÇAS VERTICAIS



$$NKJ + NKH \sin 72^\circ + NKL \sin 72^\circ = 0$$

$$0 + (-105,26 \times 0,95) + NKL \times 0,95 = 0$$

$$-105,26 \times 0,95 + NKL \times 0,95 = 0$$

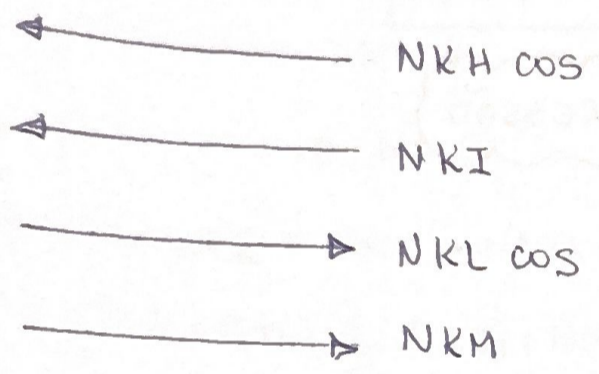
$$-99,99 + NKL \times 0,95 = 0$$

$$NKL = \frac{99,99}{0,95}$$

$$NKL = 105,26$$

TRACÇÃO

FORÇAS HORIZONTAIS



$$- NKH \cos + NKI + NKL \cos + NKM = 0$$

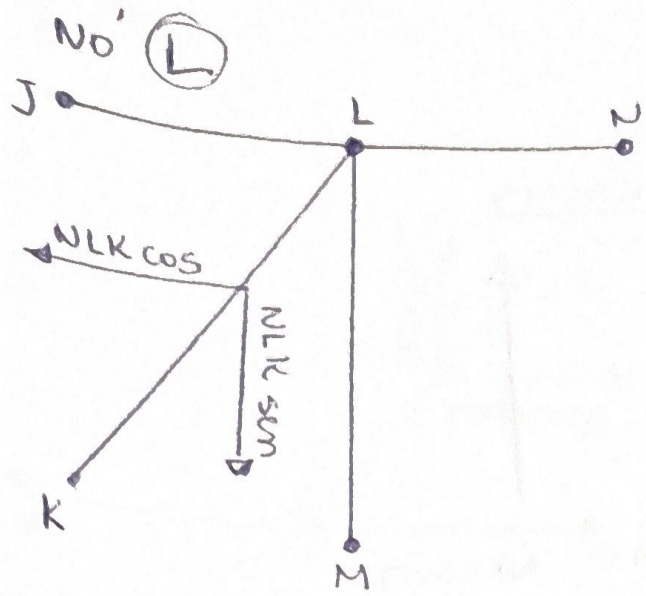
$$-(-105,26 \times 0,31) - (130,52) + (105,26 \times 0,31) + NKM = 0$$

$$+ 32,63 - 130,52 + 32,63 + NKM = 0$$

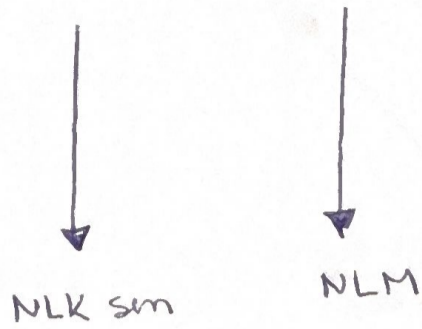
$$-65,23 + NKM = 0$$

$$NKM = 65,23$$

TRACÇÃO



FORÇAS VERTICAIS



$$-NLK \sin 72^\circ - NLM = 0$$

$$-(105,26 \times 0,95) - NLM = 0$$

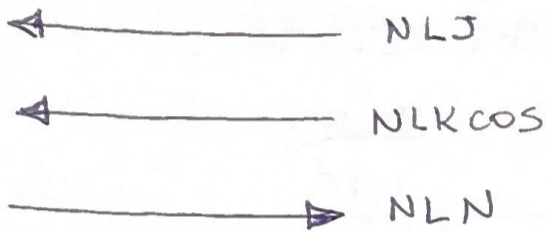
$$-99,99 - NLM = 0$$

$$-NLM = +99,99 \quad (x-1)$$

$$\boxed{NLM = -99,99}$$

COMPRESSÃO

FORÇAS HORIZONTAIS



$$-NLJ - NLK \cos 72^\circ + NLN = 0$$

$$-(-97,89) - (105,26 \times 0,31) + NLN = 0$$

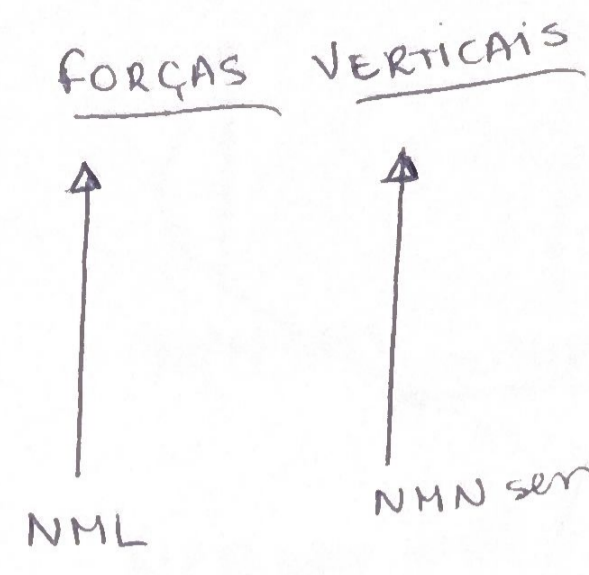
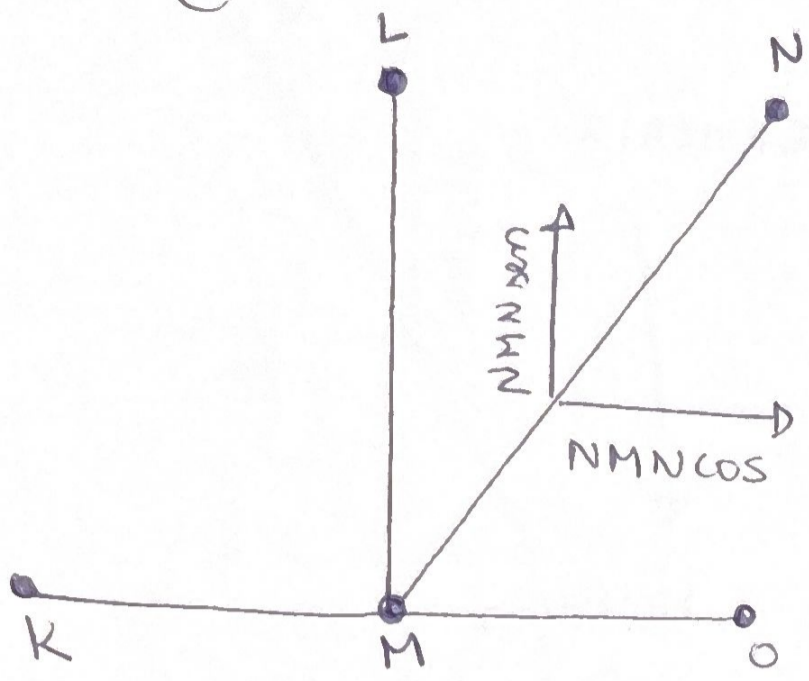
$$97,89 - 32,63 + NLN = 0$$

$$65,26 + NLN = 0$$

$$\boxed{NLN = -65,26}$$

COMPRESSÃO

No' (M)



FORÇAS VERTICAIS

$$NML + NMN \sin 72^\circ = 0$$

$$-99.99 + NMN \times 0.95 = 0$$

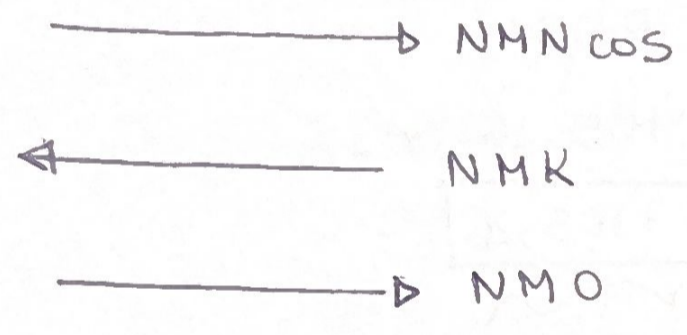
$$-99.99 + NMN \times 0.95 = 0$$

$$NMN = \frac{99.99}{0.95}$$

$$NMN = 105.26$$

TRACÃO

FORÇAS HORIZONTAIS



$$NMN \cos 72 + NMK + NMO = 0$$

$$(105.26 \times 0.31) - (65.23) + NMO = 0$$

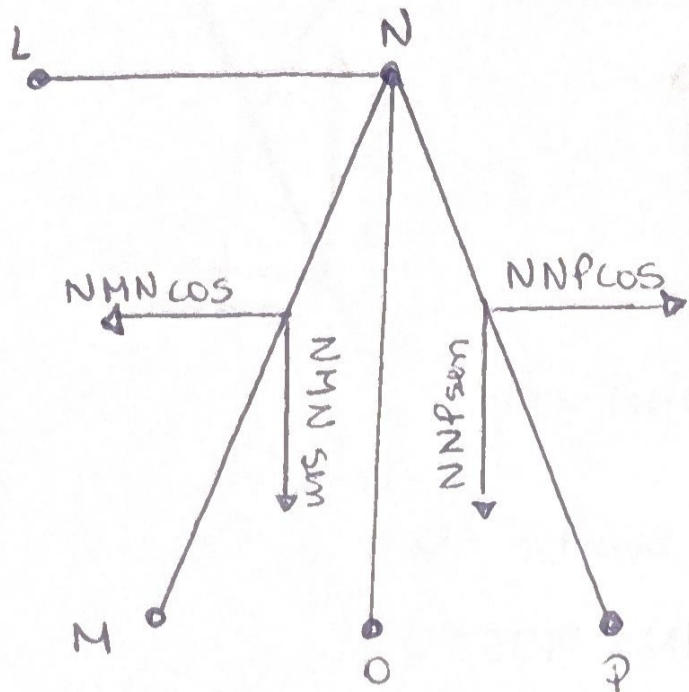
$$32.63 - 65.23 + NMO = 0$$

$$-32.63 + NMO = 0$$

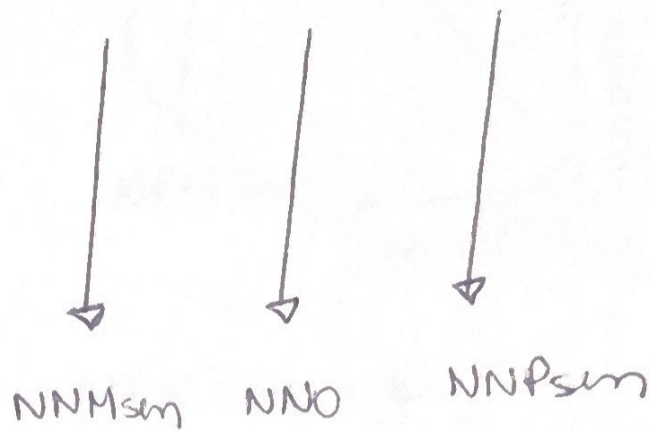
$$NMO = 32.63$$

TRACÃO

NO' (N)



FORÇAS VERTICAIS



$$-(105.26 \times 0,95) - 0 - NNP \times 0,95 = 0$$

$$- 99.99 - NNP \times 0,95 = 0$$

$$- NNP = \frac{99.99}{0.95}$$

$$- NNP = 105.26 (x-3)$$

$$\boxed{NNP = -105,26}$$

COMPRESSÃO

FORÇAS HORIZONTAIS

→ NNP cos

←>NNL

← NNM cos

$$NNP \cos 72^\circ ->NNL - NNM \cos 72^\circ = 0$$

$$(NNP \times 0,31) - (-65.26) - (105.26 \times 0,31) = 0$$

$$NNP \times 0,31 + 65.26 - 32.63 = 0$$

$$NNP \times 0,31 + 32.63 = 0$$

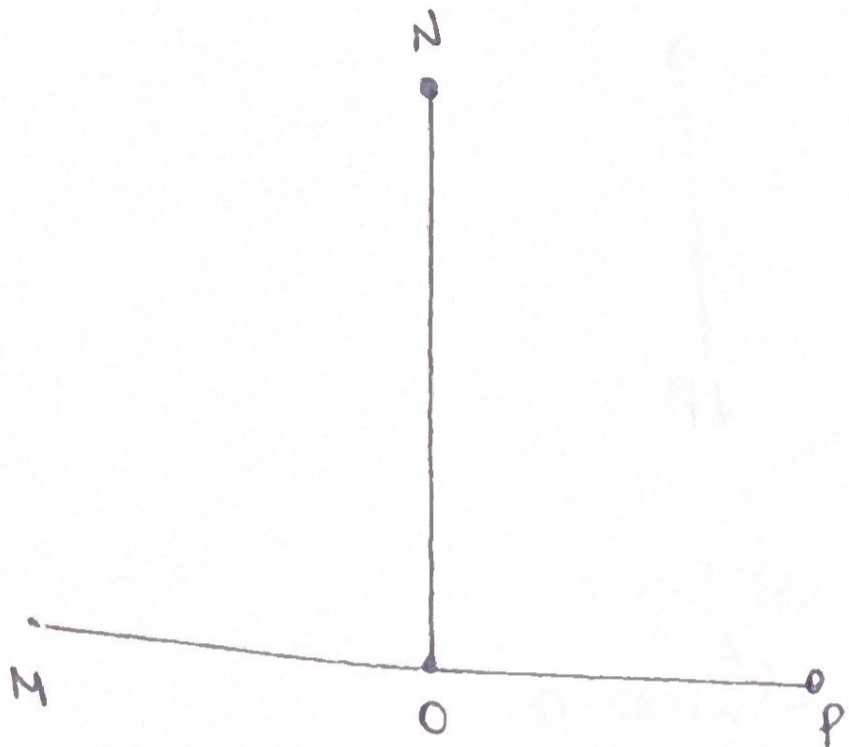
$$NNP = -\frac{32.63}{0,31}$$

$$\boxed{NNP = -105,26}$$

COMPRESSÃO

Nó (O)

9



FORÇAS VERTICAIS



$$\boxed{NON = 0}$$

FORÇAS HORIZONTAIS



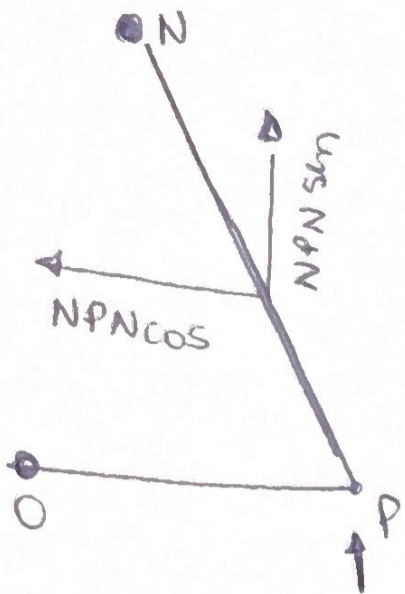
$$- NOM + NOP = 0$$

$$- (32.63) + NOP = 0$$

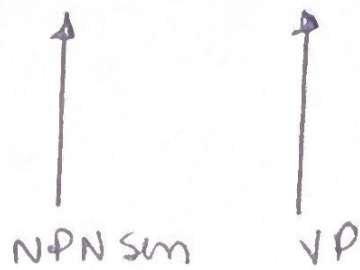
$$\boxed{NOP = 32.63}$$

TRACÇÃO

NO' (P)



### FORÇAS VERTICAIS



$$NPN \sin 72 + VP = 0$$

$$NPN \times 0,95 + 100 = 0$$

$$NPN = -\frac{100}{0,95}$$

$$\boxed{NPN = -105,26}$$

COMPRESSÃO

### FORÇAS HORIZONTAIS



$$-NPO - NPN \cos 72^\circ = 0$$

$$-(32,63) - NPN \times 0,31 = 0$$

$$-NPN = \frac{32,63}{0,31}$$

$$-NPN = 105,26 (x-1)$$

$$\boxed{NPN = -105,26}$$

COMPRESSÃO

CÁLCULO NÚMERO DE FIOS DE MACARRÃO (TRAÇÃO)

$$\frac{N}{4.267}$$

$$f = 105.26$$

$$\frac{105.26}{4.267} = 24 \text{ (12 FIOS DE CADA LADO)}$$

$$f = 65.26$$

$$\frac{65.26}{4.267} = 16 \text{ (8 FIOS DE CADA LADO)}$$

$$f = 32.63$$

$$\frac{32.63}{4.267} = 8 \text{ (4 FIOS DE CADA LADO)}$$

$$f = 199.98$$

$$\frac{199.98}{4.267} = 46 \text{ (23 FIOS DE CADA LADO)}$$

$$f = 130.52$$

$$\frac{130.52}{4.267} = 30 \text{ (15 FIOS DE CADA LADO)}$$

⑤ CÁLCULO DE NÚMERO DE FIOS DE MACARÃO (COMPRESSÃO)

①

$$\sqrt{\frac{N \cdot L^2}{27906 \times r^4}}$$

$$F = -105.26$$

$$\sqrt{\frac{-105.26 \times (420)^2}{27906 \times (0.95)^4}} = 28 \quad (14 \text{ FIOS DE CADA LADO})$$

$$F = -65.26$$

$$\sqrt{\frac{-65.26 \times (130)^2}{27906 \times (0.95)^4}} = 7 \quad (4 \text{ FIOS DE CADA LADO})$$

$$f = -99.99$$

$$\sqrt{\frac{-99.99 \times (400)^2}{27906 \times (0.95)^4}} = 26 \quad (13 \text{ FIOS DE CADA LADO})$$

$$F = -97.89$$

$$\sqrt{\frac{-97.89 \times (130)^2}{27906 \times (0.95)^4}} = 8 \quad (4 \text{ FIOS DE CADA LADO})$$





